Computational Trust

SFM'11 Bertinoro June 2011

Mogens Nielsen University of Aarhus DK



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Plan of talk

- 1) The grand challenge of Ubiquitous Computing
- 2) The role of Computational Trust in Ubiquitous Computing a brief survey
- 3) Some results towards rigorously defined models of Computational Trust

Joint work with Sassone, Palamidessi, Krukow, Carbone, Cahill,....



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Wave of Grand Challenge Initiatives

- Grand Challenges in Computer Science and Engineering
 - Computing Research Association, USA
- Fundamentals of Computer Science Challenges and Opportunities
 - National Science Foundation, USA
- Short papers on Grand Challenges in Computer Science
 - Journal of ACM 50 (1) 2003
- 2020 Future of Computing
 - Nature, 2006
- UK Grand Challenges for Computing Research
 - EPSRC and others, currently



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UK Grand Challenge

Engineering and Physical Sciences Research Council

British Computer Society

Institution of Electrical Engineers

ukcrc.org.uk/grand-challenge/index.cfm





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UK Grand Challenges in Computing Research

- 1. In Vivo <=> In Silico
- 2. Ubiquitous Computing: UbiComp

www-dse.doc.ic.ac.uk/Projects/UbiNet/GC

- 3. Memories for Life
- 4. The Architecture of Brain and Mind
- 5. Dependable Systems Evolution
- 6. Non-Classical Computation
- 7. Learning for Life
- 8. Bringing the Past to Life for the Citizen



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Visions of UbiComp

- Billions of autonomous mobile networked entities
 - Mobile users
 - Mobile software agents
 - Mobile networked devices:
 - Mobile communication devices (phones, pagers, ...)
 - Mobile computing devices (laptops, palmtops, ...)
 - Commodity products (embedded devices)
- Entities will collaborate with each other
 - Resource sharing
 - Ad hoc networks, computational grids, ...
 - Information sharing
 - Collaborative applications, recommendation systems, ...



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Data Security in UbiComp

- Data Security related properties of UbiComp
 - Large number of autonomous entities
 - Large number of administrative domains
 - No common trusted computing base
 - Virtual anonymity
- excluding the use of traditional security mechanisms used in distributed systems – e.g. passwords, certificates, keys,...!
- ONE alternative approach:
 Trust based data security



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Computational Trust - UbiComp

- Decisions related to communication made autonomously based on
 - entities' behaviour, reputation, credentials,...
 - other entities' recommendations,...
 - incomplete information, contexts, mobility,...
- Decisions related to communication made autonomously based on
 - a suitable computational notion of trust in order to achieve some required properties of communication between entities



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- 3) Some results towards rigorously defined models of Computational Trust



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Trust Surveys

- Trust in the Social Sciences
 - D. H. McKnight, N.L. Chervany: The Meaning of Trust, Trust in Cyber-societies, Springer LNAI 2246, 2001



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McKnight and Chervany

- TRUST
- Disposition
- Structural
- Affect/Attitude
- Belief/Expectancy
- Intention
- Behaviour

- TRUSTEE
- Competence
- Benevolence
- Integrity
- Predictability
- Openness, carefulness,...
- People, Institutions,...



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Computational Trust Surveys

- Computational Trust in UbiComp
 - T. Grandison, M. Sloman: A Survey of Trust in Internet Applications, IEEE Communications Surveys & Tutorials, 3(4), 2000
 - J. Sabater, C. Sierra: Review on Computational Trust and Reputation *Models*, Artificial Intelligence Review, 24, 33-60, 2005
 - A. Jøsang, R. Ismail, C. Boyd: A Survey of Trust and Reputation for Online Service Provision, Decision Support Systems, 43(2), 2006



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Jøsang et al: Computational Trust

- Find adequate online substitutes for the traditional cues to trust and reputation from the physical world and identify information elements (specific to a particular online application) which are suitable for deriving measures of trust and reputation
- Take advantage of IT and the internet to create efficient systems for collecting that information, and for deriving measures of trust and reputation, in order to support decision making and to improve the quality of online markets



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Jøsang et al: Trust semantics

- Trust values:
 - Discrete trust values
 - Summation or average of ratings
 - Probabilistic systems
 - Belief models
 - Fuzzy models
 - Flow models



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Jøsang et al: Commercial systems

- Specific versus General
- Subjective versus Objective
- eBay's Feedback Forum
- Amazon
- Google Page Ranking



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Computational Trust Applications

- Information provider applying trust in requesters
 - e.g. should I allow requester R to access my resource r?
 - Data security, Access control,...
- Information requester applying trust in providers
 - e.g. which of providers *P*, *Q*, *R*,... will provide the best service *s* for me?
 - Quality of services,...



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Computational Trust Systems

- Credential based
 - the KeyNote System of Blaze et al
 - the *Delegation Logic* of Li et al
 -
- Reputation based
 - the Beta Reputation System of Jøsang et al
 - the Eigentrust System of Kamvar et al
 -



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Computational Trust

- Trust formation
 - Individual experience
 - Recommendation from known (trusted) third parties
 - Reputation (recommendation from many strangers)
- Trust evolution
 - Incorporating new trust formation data
 - Expiration of old trust values
- Trust exploitation
 - Risk analysis
 - Feedback based on experience
 - Context dependence



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UbiComp Challenges

- Science Goal
 - to develop a coherent informatics science whose concepts, calculi, models, theories and tools allow descriptive, explanatory and predictive analysis of ubiquitous computing at many levels of abstraction
 - to employ these theories to derive all its systems and software, including languages
 - to analyse and justify all its constructions by these theories and tools



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UbiComp: Computational Trust

- On trust:
 - "..trust between autonomous agents will be an important ingredient..... A discipline of trust will only be effective if it is rigorously defined..."
- On rigorously defined:
 "...tools for formalization, specification, validation, analysis, diagnosis, evaluation,"



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Plan of talk

- 1) The grand challenge of Ubiquitous Computing
- 2) The role of Computational Trust in Ubiquitous Computing a brief survey
- 3) Some results towards rigorously defined models of Computational Trust
 - a) Trust in requesters based on credentials
 - b) Trust in providers based on reputation



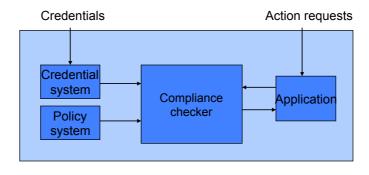
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Trust management elements

- Language for Actions
- Naming scheme for Principals
- Language for Trust-Policies
- Language for Credentials
- Compliance checker and interface
- Blaze, Feigenbaum, Ioannidis, Keromytis: The Role of Trust Management ion Distributed Systems Security, Springer LNCS 1603, 185-210, 1999
- Li, Mitchell: A Role-based Trust-management Framework, DISCEX III, IEEE Computer Society Press, 2003



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Trust policies

- Each principal defines a trust policy which declares how it computes its trust in every other principal
- A small policy language could have constructs like
 - Refer to the information registered locally
 - Refer to information registered by other principals
 - Refer to the information P would obtain if it were to compute its trust
 - Other operations...



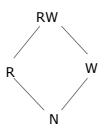
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Example: A simple trust setting

• Let *T* be {N, R, W, RW}





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. . . .

Example trust policies

b: $\lambda x. \ (x=c \Rightarrow W_{,...})$ abstraction

a: λx . ([b]x V R) referencing

a: λx . (([a]b \wedge [b]x) V R) discounting

 $a: \lambda x. (\lceil b \rceil x)$

b: λx . ($\lceil a \rceil x$) cyclic delegation



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Modeling Trust

- Scenario with
 - A set \mathcal{P} of principals (ranged over by a,b,c)
 - A set T of trust values
- Trust information of a system represented by
 - trust-state: $P \rightarrow P \rightarrow T$
 - trust-state(A)(B): represents A's trust in B



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Modeling the web of Trust

Each Principal specifies a *policy* which is a local contribution to the global trust

Given principals a with policies π_a :

$$\pi_a : \left[\ \mathcal{P} \to \mathcal{P} \to \mathcal{T} \right] \to \left[\ \mathcal{P} \to \mathcal{T} \right]$$

The collection of π_a 's induces a global trust function:

$$\Pi: \left[\ \mathcal{P} \to \mathcal{P} \to \mathcal{T} \right] \to \left[\mathcal{P} \to \mathcal{P} \to \mathcal{T} \right]$$



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Definition of Trust

Assume T is a lattice/cpo, given a ≤-continuous global trust function

$$\Pi: \left[\ \mathcal{P} \to \mathcal{P} \to \mathcal{T} \right] \to \left[\mathcal{P} \to \mathcal{P} \to \mathcal{T} \right]$$

TRUST is defined as the *least fixed-point* of Π

Weeks: *Understanding Trust Management Systems,* IEEE Symposium on Security and Privacy, 2001



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Lattices and continuity

In a complete lattice $T = (D, \leq)$ all subsets X of D have a least upper bound $\cup X$ and a greatest lower bound $\cap X$

```
F: D \rightarrow D is \leq-continuous iff F(\cup X) = \cup F(X) implying that F is \leq-monotone F: D \rightarrow D is \leq-monotone iff X \leq Y => F(X) \leq F(Y)
```

For $F: D \to D \le continuous$, the least fixed point of F exists and is equal to $\cup F^i(\bot)$



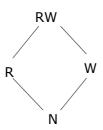
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Example: A simple trust setting

• Let \mathcal{T} be $\{N, R, W, RW\}$





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Example (1)

Suppose we have the following policies:

	а	b	С
d	[<i>f</i>] V W	[e] ∧ W	N
е	R	R	[<i>f</i>]
f	[e]	N	[e]



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Example (2)

• The computation:

	а	b	С
d	[<i>f</i>] V W	[e] / W	N
е	R	R	[<i>f</i>]
f	[e]	N	[e]

	а	b	С
d	[N,RW]	[N,RW]	[N,RW]
е	[N,RW]	[N,RW]	[N,RW]
f	[N,RW]	[N,RW]	[N,RW]



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mana Nilalaa

Example (3)

• The computation:

	а	b	С
d	[<i>f</i>] V W	[e] / W	N
е	R	R	[<i>f</i>]
f	[e]	N	[e]

	а	Ь	С
d	[W,RW]	[N,W]	[N,N]
е	[R,R]	[R,R]	[N,RW]
f	[N,RW]	[N,N]	[N,RW]



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Example (4)

• The computation:

	а	b	С
d	[<i>f</i>] V W	[e] ∧ W	N
е	R	R	[<i>f</i>]
f	[e]	N	[e]

	а	b	С
d	[W,RW]	[N,N]	[N,N]
е	[R,R]	[R,R]	[N,RW]
f	[R,R]	[N,N]	[N,RW]



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Example (5)

• The computation:

	а	b	С
d	[<i>f</i>] V W	[e] / W	N
е	R	R	[<i>f</i>]
f	[e]	N	[e]

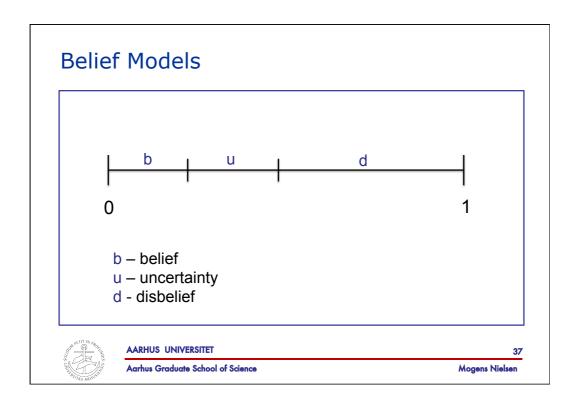
	а	Ь	С
d	[RW,RW]	[N,N]	[N,N]
е	[R,R]	[R,R]	[N,RW]
f	[R,R]	[N,N]	[N,RW]



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Trust domain

- T is equipped with two orderings ≤ and ≤ where
- ≤ represents information ordering
- ≤ represents trust ordering



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Example: Proof carrying requests

 Idea: Assume r sending a request to a, requiring high trust

```
a: \lambda x. (\lceil b \rceil x \lor \dots)
b: \lambda x. (x=r \Rightarrow high,\dots)
```



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Example: Proof carrying request

Theorem

Assume that \leq is \leq -continuous and that Π is \leq -monotone

Given $m: \mathcal{P} \to \mathcal{P} \to \mathcal{T}$, if

- *m* ≤ ⊥<
- $m \leq \Pi(m)$

then $m \leq lfp_{\leq} \Pi$



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Example: Proof carrying request

- Idea: Requester provides m along with his request (sufficient for the request to be met) as an argument for m ≤ lfp_≤ Π
- Send m to all principals a for which m(a) is different from $\lambda p. \bot_{<}$, and ask a to check that $m \le \pi_a(m)$
- If this is the case for all such principals, conclude that $m \le \Pi(m)$, and hence $m \le \mathrm{lfp}_\le \Pi$



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Example: Proof carrying requests

 Idea: Assume r sending a request to a, requiring high trust

```
a: \lambda x. (\lceil b \rceil x \lor \dots)
b: \lambda x. (x=r \Rightarrow high,\dots)
```



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Trust in Providers – Based on Reputations EigenTrust Algorithm - Kamvar et al

- Peers (i,j,..) interact and mutually rate interactions as being either satisfactory or unsatisfactory:
 - $s_{ij} = max (N_{sat}(i,j) N_{unsat}(i,j), 0)$
- These ratings are normalised
 - $c_{ij} = s_{ij} / \Sigma_j s_{ij}$
- [c_{ij}] is a Markov chain with stationary distribution [t_j]
 interpreted as the global trust in peer j



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EigenTrust Algorithm for P2P Networks

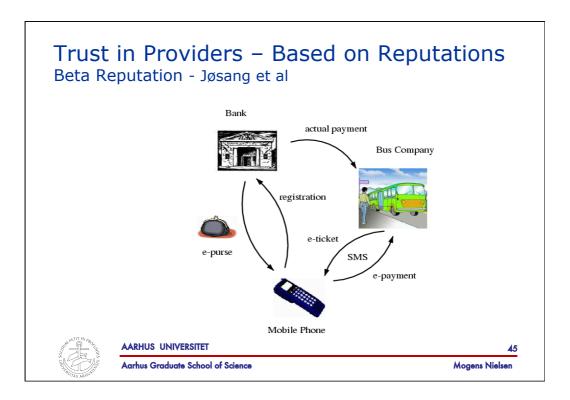
- System simulations show that EigenTrust can significantly reduce the number of non-authentic file downloads in a P2P filesharing system, even when up to 70% of the peers maliciously cooperate
- But what is Eigentrust computing, e.g. what does it mean that the trust in some peer is .75?
- Kamwar, Schlosser, Garcia-Molina: The Eigentrust Algorithm for Reputation Management in P2P Networks, proceedings of WWW'03, ACM Press, 640-651, 2003



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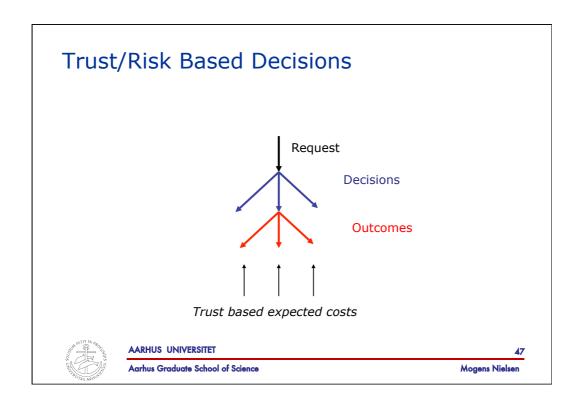
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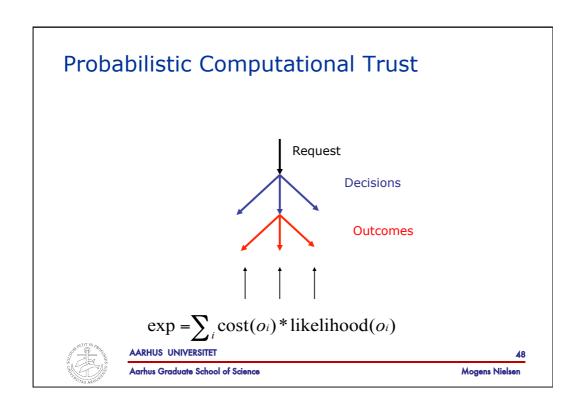


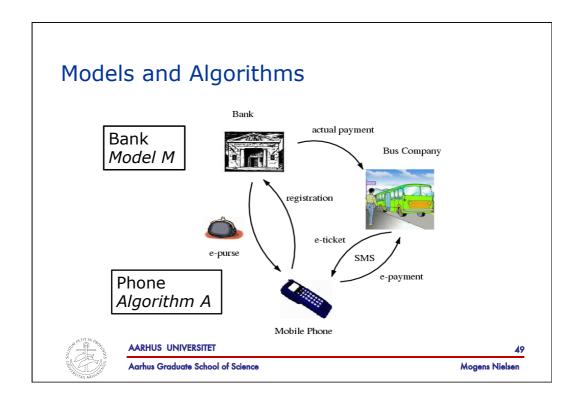
E-Purse Scenario

- Consider a situation where a user is considering requesting an amount m of e-cash from a bank
- Seen from the point of view of the user, an "untrusted" bank may
 - deny the request, e.g. because the bank server is down for maintenance
 - grant the request, but withdraw an amount different from m from users account
 - grant the request, but the transferred e-cash may be forged









Probabilistic Models for Computational Trust

- Given a (finite) set of outcomes of interactions
 - $O = \{o_1, o_2, ..., o_m\}$
- A probabilistic model M of principal behaviour defines for $h \in O^*$ and $o_i \in O$
 - P(h | M) the probability of observing h in M
 - $P(o_i \mid h \mid M)$ the probability of o_i in the next interaction given observation h in M



Probabilistic Computational Trust Algorithms

- Given a (finite) set of outcomes of interactions
 - $O = \{o_1, o_2, ..., o_m\}$
- A probabilistic computational trust algorithm A
 - takes as input a history $h \in O^*$ and
 - outputs a probability distribution on O $A(o_i \mid h) \in [0,1]$ for i = 1,2,...,m



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The Goal for Probabilistic Trust Algorithms

- Algorithm A producing A(o_i | h) should approximate Model M probabilities P(o_i | h M) as well as possible!
- Notice that this gives rise to rigid versions of soft correctness question:
 - how well does a particular algorithm approximate the model?
 - how robust is it wrt. the model and its parameters?



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A Concrete Simple Probabilistic Model

- The Bernoulli Model $M_B(\theta)$
 - Assume that the behaviour of a particular principal, p, has only two outcomes, with a probability θ for success (and 1- θ for failure)
- Algorithm A
 - Output: a probability distribution $\{s, f\} \rightarrow [0, 1]$
- The Goal
 - A should approximate $(\theta \ 1- \theta)$ as well as possible



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Probabilistic Trust Algorithms

- Focus on two example algorithms:
 - P2P Reputation Management of Despotocvic et al
 - Computational Model for eBusiness of Mui et al



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Despotovic et al 2004: Algorithm A_D

- The Specification (of trust computation algorithm A)
 - Input: a sequence of observations $h = x_1x_2...x_n \in \{s, f\}^*$
 - Output: a probability distribution $\{s, f\} \rightarrow [0, 1]$
- The algorithm A_D for $M_B(\theta)$
 - $\bullet \ A_D(s \mid h) = N_s(h) / |h|$
 - $\bullet A_D(f \mid h) = N_f(h) / |h|$
- Despotovic, Aberer: A Probabilistic Approach to Predict Peers' Performance in P2P Networks, CIA'04, Springer LNCS 3192, 62-76, 2004



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Mui et al 2002: Algorithm A_M

- The Specification (of trust computation algorithm A)
 - Input: a sequence of observations $h = x_1x_2...x_n \in \{s, f\}^*$
 - Output: a probability distribution $\{s, f\} \rightarrow [0, 1]$
- The algorithm A_M :
 - $A_M(s \mid h) = (N_s(h) + 1) / (|h| + 2)$
 - $A_M(f \mid h) = (N_f(h) + 1) / (|h| + 2)$
- Mui, Motashemi, Halberstadt: A Computatinal Model of Trust and Reputation for eBusinesses, HICSS'02, IEEE Press, 2002



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A Question: how to choose

- The Goal
 - Algorithm A should approximate $(\theta_{_{_{/}}} 1$ $\theta)$ as well as possible
- Which of the two algorithms A_D and A_M performs best relative to this goal?
 - Experimental approach: answers given based on experiments in simulation environments
 - Theoretical approach: answer given in terms of mathematical results in our probability model



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How to measure "approximate"?

- The "distance from a true distribution \boldsymbol{p} to an approximation \boldsymbol{q}'' (here on $O = \{o_1, o_2, ..., o_m\}$) can be measured as e.g
 - the Relative Entropy (also called the Kullback-Leibler divergence):

$$D(\mathbf{p} \mid\mid \mathbf{q}) = \sum_{i} \mathbf{p}(o_{i}) \times \log_{2}(\mathbf{p}(o_{i}) / \mathbf{q}(o_{i}))$$

- $D(\mathbf{p} || \mathbf{q}) = \Sigma_i (\mathbf{p}(o_i) \mathbf{q}(o_i))^2$
- Results holds for e.g. both these choices



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The Goal of a Probabilistic Algorithm: Formally

- The Goal
 - Algorithm A producing A(o_i | h) should approximate P(o_i | h M) as well as possible
- We choose to interpret "as well as possible" in terms of the expected distance between the two distributions:

$$ED^{n}(\mathbf{M} \mid\mid \mathbf{A}) = \sum_{h \in \mathcal{O}}^{n} p(h \mid \mathbf{M}) \times D(P(\cdot \mid h\mathbf{M}) \mid\mid \mathbf{A}(\cdot \mid h))$$



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How to choose: Formally

• Comparing A_D and A_M against M_B :

If
$$\theta = 0$$
 or $\theta = 1$ then for all n
 $ED^n(M_B(\theta), A_D) = 0 < ED^n(M_B(\theta), A_M)$

If
$$0 < \theta < 1$$
 then for all n
 $ED^{n}(M_{B}(\theta), A_{M}) < ED^{n}(M_{B}(\theta), A_{D}) = \infty$



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Bayesian Approach

Bayes' theorem:

$$P(\theta \mid h,M) = P(\theta \mid M) \times (P(h \mid \theta,M) / P(h \mid M))$$

- For the model M_B choosing
 - $P(\theta \mid M_B)$

=
$$Beta(a, \beta) (\theta)$$

- Beta $(a, \beta)(\theta) = \theta^{a-1} (1-\theta)^{\beta-1} \Gamma(a+\beta) / \Gamma(a) \Gamma(\beta)$
- Allows the following simple "algorithms" computing the a posteriori information
 - $P(\theta \mid h, M_B)$ = $Beta(a + N_s(h), \beta + N_f(h))$
 - $E(Beta(a, \beta)) = a/(a + \beta)$

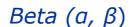


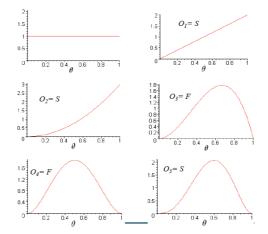
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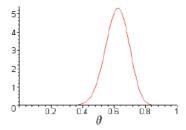


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Beta (a, β) – after 25 "S" and 15 "F"





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Two Examples Generalised

- A_D the P2P Reputation Management of Despotocvic et al
 - an example of the Bayesian approach with $a=\beta=0$
- A_M the Computational Model for eBusiness of Mui et al
 - an example of the Bayesian approach with $a=\beta=1$
- Generalize to all symmetric Beta priors, i.e. for arbitrary real numbers $\varepsilon \ge 0$:
 - $A_{\varepsilon}(s \mid h) = (N_s(h) + \varepsilon) / (|h| + 2\varepsilon)$
 - $A_{\varepsilon}(f \mid h) = (N_{f}(h) + \varepsilon) / (|h| + 2\varepsilon)$
- What is a good choice of ε and how does this choice depend on θ and n?



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Some Theoretical Answers: how to choose

For any $\theta \in [0,1]$, $\theta \neq 1/2$, there exists an ε_{θ} which for any n minimizes $ED^n(M_B(\theta), A_{\varepsilon})$. Furthermore, ε_{θ} is defined as the following function of θ

$$\varepsilon_{\theta} = 2\theta(1-\theta) / (2\theta-1)^2$$

Meaning: unless behaviour is completely random, there is a unique best algorithm (choosing $\varepsilon := \varepsilon_{\theta}$) outperforming all other A_{ε} algorithms, $\varepsilon \geq 0$



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Some Theoretical Answers: Robustness

Furthermore, $ED^n(M_B(\theta), A_{\varepsilon})$ is continuous (as a function of ε) – decreasing on the interval $(0, \varepsilon_{\theta})$ and increasing on $(\varepsilon_{\theta}, \infty)$

Meaning: The closer ε is to ε_{θ} the better performance of A_{ε}



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Some Theoretical Answers: how to choose

Given a particular ε_r , the algorithm A_{ε} is an optimal choice (for all n, and amongst all the A_{ϵ} algorithms) for

$$\theta = \frac{1}{2} + \frac{1}{2} \operatorname{sqrt}(2\varepsilon + 1)$$

Example: A_M is optimal for $\theta = \frac{1}{2} + \frac{1}{\sqrt{sqrt(12)}}$



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Non-symmetric priors

- Using the prior $Beta(a, \beta)$ yields the following algorithm computing the mean of the posterior distribution:

 - $A_{\alpha,\beta}$ (s | h) = $(N_s(h) + \alpha) / (|h| + a + \beta)$ $A_{\alpha,\beta}$ (f | h) = $(N_f(h) + \beta) / (|h| + a + \beta)$
- How to choose the parameters α and β ?



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Non-symmetric priors

- Assume the true behaviour (M_B) to be $Beta(a_t, \beta_t)$, define the "risk" of an algorithm $A_{a,\beta}$
- $R^n(A_{\alpha,\beta}) = \int_{[0:1]} Beta(a_t, \beta_t) ED^n(M_B(\theta), A_{\alpha,\beta}) d\theta$
- Theorem For all n, $R^n(A_{\alpha,\beta})$ is minimum for $a=a_t$ and $\beta=\beta_t$



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Non-symmetric priors

- Assume no knowledge of the true behaviour (θ in M_B), define the "risk" of an algorithm $A_{\alpha,\beta}$
- $R^n(A_{\alpha,\beta}) = \int_{[0:1]} ED^n(M_B(\theta), A_{\alpha,\beta}) d\theta$
- Theorem For all n, $R^n(A_{\alpha,\beta})$ is minimum for $\alpha = \beta = 1$



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Many More Issues to be Modelled....

- Trust formation
 - Individual experience
 - Recommendation from known (trusted) third parties
 - Reputation (recommendation from many strangers)
- Trust evolution
 - Incorporating new trust formation data
 - Expiration of old trust values
- Trust exploitation
 - Risk analysis
 - Feedback based on experience
 - Context dependence



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Thank you for your attention!



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